

lation coefficients between the directions of rays and the number of narrow pairs in nuclear disintegrations. Using the table of random stars it is possible to obtain the theoretical values of these quantities. The number of pairs with angle  $\leq 2^\circ$  (see Fig. 3) was equal to four in 200 stars. This is close to the quantity obtained in reference 6. The  $Q$  values (see reference 6, Table I, last line) connected with the correlation coefficients were, respectively,  $0.32 \pm 0.06$ , and  $0.00 \pm 0.07$ . A more detailed analysis of the correlations showed that as the number of rays in the stars increased, the statistical dependence between the directions of the rays becomes more obvious. This is connected with an increase of the limits placed on the directions of the particles by the law of conservation of momentum.

These results from the formation of the table of random stars testifies to the usefulness of this method for analyzing various details of the process of multiple production.

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### TEMPERATURE DEPENDENCE OF FERROMAGNETIC RESONANCE IN YTTRIUM FERRITE-GARNETS

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THERE have hitherto been few data on the temperature dependence of ferromagnetic resonance in ferrites. Meanwhile, the study of this dependence has acquired considerable importance, because it is here that the relation between the resonance characteristics and the magnetic properties of a ferrite is manifested most clearly. The present communication presents the results of a study of the temperature dependence of the width of the ferromagnetic resonance absorption line, the  $g$ -factor, and the resonance field in polycrystalline yttrium ferrite-garnets, in which the  $Fe^{3+}$  ions have been partly replaced by  $Al^{3+}$  and  $Cr^{3+}$  ions. At the same time, measurements of the temperature dependence of the spontaneous magnetization were made by a method described earlier.<sup>1</sup>

Figure 1 shows the temperature dependence of the absorption line width (solid curves) and of the specific spontaneous magnetization (dashed curves) of yttrium ferrite-garnets of the follow-

ing compositions:  $3Y_2O_3 \cdot 5Fe_2O_3$  (1);  $3Y_2O_3 \cdot 4Fe_2O_3 \cdot Al_2O_3$  (3);  $3Y_2O_3 \cdot 4.5Fe_2O_3 \cdot 0.5Cr_2O_3$  (2). Because of the small density of the specimens, the width of the resonance line was quite large; this permitted a clearer exhibition of its change on heating. It is clear from Fig. 1 that the decrease of spontaneous magnetization on approach to the Curie point occurs more abruptly than does the decrease of  $\Delta H$ . It should furthermore be noted that the decrease of  $\sigma_s$  and of  $\Delta H$  proceeds more rapidly in the case of the stoichiometric ferrite  $3Y_2O_3 \cdot 5Fe_2O_3$  than it does for the "substituted" ferrites. The greater the  $Al^{3+}$  and  $Cr^{3+}$  content, the more slanting the  $\Delta H$  and  $\sigma_s$

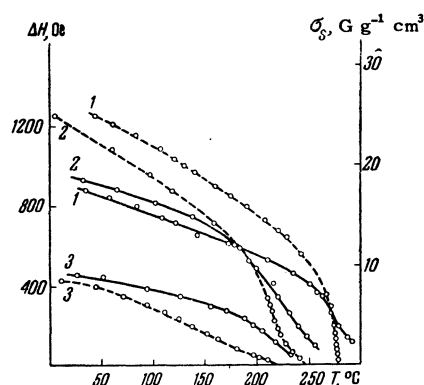


FIG. 1. Temperature dependence of the width  $\Delta H$  of the ferromagnetic resonance absorption line (solid curves) and of the specific spontaneous magnetization  $\sigma_s$  (dashed curves): 1) for  $3Y_2O_3 \cdot 5Fe_2O_3$ ; 2) for  $3Y_2O_3 \cdot 4.5Fe_2O_3 \cdot 0.5Cr_2O_3$ ; 3) for  $3Y_2O_3 \cdot 4Fe_2O_3 \cdot Al_2O_3$ .

curves are in comparison with the curves for  $3Y_2O_3 \cdot 5Fe_2O_3$ . Probably the  $Al^{3+}$  and  $Cr^{3+}$  ions are distributed nonuniformly in the ferrite-garnet lattice, as a result of which there occur fluctuations of the exchange interactions through the volume of the specimen; these in turn lead to a "washing out" of the curves of  $\Delta H$  and  $\sigma_S$  vs temperature. According to the theory of Clogston, Suhl, et al.,<sup>2</sup> the value of  $\Delta H$  in ferrites should be proportional to  $\sqrt{\sigma_S}$ . As can be seen from Fig. 2, this

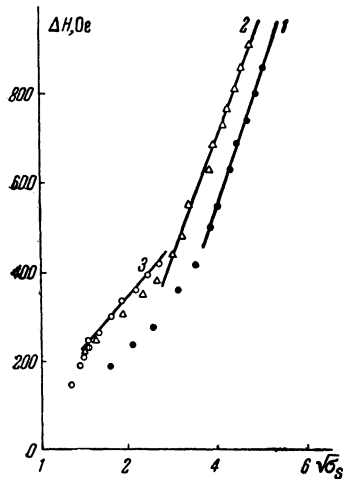


FIG. 2. Dependence of  $\Delta H$  on  $\sqrt{\sigma_S}$  for ferrite-garnets, calculated from the curves of Fig. 1 (same materials and same notation for them).

relation is satisfied qualitatively in a certain temperature interval (far from the Curie point).

Figure 3 shows the temperature dependence of

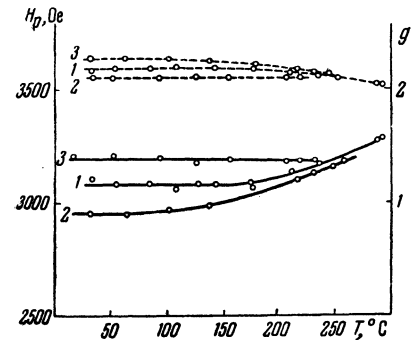


FIG. 3. Temperature dependence of resonance field  $H_p$  (solid curves) and of  $g$ -factor (dashed curves) for the same materials as in Fig. 1.

the resonance field  $H_p$  and of the  $g$ -factor on temperature. It is interesting to note that in the stoichiometric ferrite  $3Y_2O_3 \cdot 5Fe_2O_3$  and in  $3Y_2O_3 \cdot 4.5Fe_2O_3 \cdot 0.5Cr_2O_3$ ,  $H_p$  increases on approach to the Curie point, whereas the  $g$ -factor decreases slightly.

This work was performed under the direction of K. P. Belov.

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### MAGNETIC AND RESONANCE PROPERTIES OF YTTRIUM FERRITE-GARNETS WITH REPLACEMENT OF $Fe^{3+}$ IONS BY $Cr^{3+}$ AND $Al^{3+}$ IONS

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RECENTLY there has been great interest in the investigation of ferromagnetic resonance in new magnetic materials, ferrite-garnets of the rare-earth elements and of yttrium.<sup>1,2</sup> In the present communication we give the results of our experiments on the effect of replacement of  $Fe^{3+}$  ions by  $Al^{3+}$  and  $Cr^{3+}$  ions, in the stoichiometric yttrium ferrite-garnet  $3Y_2O_3 \cdot 5Fe_2O_3$ , upon the magnetic and resonance properties of this ferrite. Upon replacement of a corresponding quantity of

$Fe^{3+}$  ions by  $Al^{3+}$  and  $Cr^{3+}$ , the formulas for the ferrites studied will have the form:

$$3Y_2O_3 \cdot (5 - a) Fe_2O_3 \cdot a Al_2O_3; 3Y_2O_3 \cdot (5 - a) Fe_2O_3 \cdot a Cr_2O_3.$$

Here  $a$  is the content of  $Al^{3+}$  or  $Cr^{3+}$  ions per mole. The measurements of magnetic and resonance characteristics were carried out on polycrystalline specimens, prepared in accordance with standard ceramic technology (sintering at 1300°C in air for four hours). The density of the specimens was no greater than 2.75 g/cm<sup>3</sup>; this led to a pronounced broadening of the ferromagnetic resonance absorption line. In our experiments this was an advantage, since it permitted a clear exhibition of the effect of the introduction of  $Al^{3+}$  and  $Cr^{3+}$  ions into the ferrite upon the absorption line width. For all the specimens, isotherms of the magnetization were taken by a ballistic method at helium temperatures; from these the saturation magnetization  $\sigma_0$  was found, in Bohr magnetons per mole.

Replacement of  $Fe^{3+}$  ions by  $Al^{3+}$  ions (which have no magnetic moment) causes a decrease in the value of  $\sigma_0$  (Fig. 1), whereas replacement by  $Cr^{3+}$  ions at first leads to an increase of  $\sigma_0$ ; but